

Solubility of  $\text{Ag}_2\text{O}$  in  $\text{Na}_2\text{O-B}_2\text{O}_3$  Melts

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The solubility of silver oxide in  $\text{Na}_2\text{O-B}_2\text{O}_3$  melts was determined as a function of the  $\text{Na}_2\text{O}$  contents, the temperature ( $825^\circ\text{C}$ — $935^\circ\text{C}$ ), and the oxygen partial pressures. The results show that the silver oxide dissolves in a borate as a network modifier, just like alkali metal oxides, which destroy the B—O—B bonds to produce four coordinated boron as well as three. In the  $\text{Ag}_2\text{O-B}_2\text{O}_3$  binary system, the solubility of silver oxide increases with an increase in the oxygen partial pressures. In the  $\text{Ag}_2\text{O-Na}_2\text{O-B}_2\text{O}_3$  ternary system, the solubility of  $\text{Ag}_2\text{O}$  decreases with an increase in the  $\text{Na}_2\text{O}$  contents. This shows that the silver oxide is a weaker base than sodium oxide. The activity of the oxygen ion,  $a_{\text{O}^{2-}}$ , was determined from the iso-activity lines of silver oxide. In a constant basic oxide content,  $a_{\text{O}^{2-}}$  increases with an increase in the  $\text{Na}_2\text{O}$  content. By extrapolating the  $\text{Ag}_2\text{O}$  contents to zero, the oxygen-ion activity in the  $\text{Na}_2\text{O-B}_2\text{O}_3$  melt was determined.

Molten oxides are quite interesting because of their special structures and have been studied from various aspects. The borates are especially distinguishable from such other mixed oxides as phosphates and silicates because of their structures. The boron atom can coordinate four oxygen atoms as well as three. Therefore, the borate melts show an exceptional behavior known as the boron anomaly.

Various attempts to explain the structure of molten oxides have been made. Lux and Flood<sup>1,2)</sup> explained the thermodynamic properties in terms of acidity and basicity. Krogh-Moe<sup>3,4)</sup> and Bray *et al.*<sup>5)</sup> studied the structure of borate with techniques of X-ray, NMR, and phase diagrams and measured the ratio of four to three-coordinated boron atoms with various contents of alkali metal oxide. Shartsis *et al.*<sup>6,7)</sup> measured the density, viscosity, and electrical resistivity of molten alkali borates.

The present work was performed in order to clarify whether silver oxide dissolves in a boron oxide as a network modifier and in order to examine the behavior of silver oxide in the presence of sodium oxide. The solubility of silver oxide in

$\text{B}_2\text{O}_3$  has already been measured by Willis and Hennessy.<sup>8)</sup>

Another aim of this investigation was related to the basicity of oxide melts. The oxygen-ion activity in an oxide melt is an important factor, since the basicity of the melts, which varies with the melt composition and kind of basic oxide, is supposed to be determined by this quantity. Pearce<sup>9)</sup> measured the solubility of carbon dioxide and obtained the oxygen-ion activity in soda-silica melts. In this work the oxygen-ion activity was determined from the solubility measurements of  $\text{Ag}_2\text{O}$  in the  $\text{Na}_2\text{O-B}_2\text{O}_3$  system.

## Experimental

(a) **Material and Preparation.** Samples were prepared from commercial chemicals of a guaranteed reagent grade. Their impurities were as follows;  $\text{SO}_4 < 0.003\%$ , heavy metals  $< 0.001\%$ , and  $\text{Fe} < 0.002\%$  for  $\text{B}_2\text{O}_3$ ;  $\text{SO}_4 < 0.002\%$ ,  $\text{Cu} < 0.0005\%$ , and  $\text{Fe} < 0.002\%$  for  $\text{AgNO}_3$ ;  $\text{Cl} < 0.001\%$ ,  $\text{SO}_4 < 0.002\%$ , and  $\text{PO}_4 < 0.002\%$  for borax.

To prepare the  $\text{Na}_2\text{O-B}_2\text{O}_3$  mother melt, a suitable quantity of boric oxide and borax were melted in a platinum crucible.

(b) **Chemical Analysis.** For the determination of silver, a weighed sample of glass was dissolved in dilute  $\text{HNO}_3$  and then the solution was titrated with standardized KSCN. The  $\text{B}_2\text{O}_3$  was determined in the following way. The sample was dissolved in dilute nitric acid and the pH was adjusted with *p*-nitrophenol. Glycerol was then added, and the  $\text{B}_2\text{O}_3$  was titrated with an NaOH standard solution.

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9) M. Pearce, *J. Am. Ceram. Soc.*, **47**(7), 342 (1964).

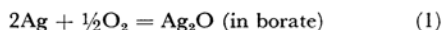
- 1) H. Lux, *Z. Electrochem.*, **45**, 303 (1939).
- 2) H. Flood and T. Forland, *Acta Chem. Scand.*, **1**, 592 (1947).
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(c) **Oxygen Pressure.** A gas mixture of oxygen and nitrogen, the oxygen partial pressure of which has previously been determined by being introducing it into the gas chromatograph at appropriate time intervals, was bubbled through the melt during each run.

(d) **Temperature.** The temperature was controlled with an Okura EC-51-type controller. During every run, the temperature was kept constant within  $\pm 1^\circ\text{C}$ .

(e) **Procedure.** The method of Willis and Hennesy was employed. The sample melt was inserted in an Ag crucible and heated in an atmosphere containing oxygen of various partial pressures.

The solution reaction can be expressed by:



The equilibrium constant,  $K$ , is defined by:

$$K = a_{\text{Ag}_2\text{O}} / \sqrt{P_{\text{O}_2}} a_{\text{Ag}}^2 \quad (2)$$

at a given temperature.

Since  $a_{\text{Ag}}$  is set at unity under the present experimental condition,  $a_{\text{Ag}_2\text{O}}$  is directly proportional to the square root of the equilibrium oxygen partial pressure. Further, it is convenient to define the standard state of  $\text{Ag}_2\text{O}$  as the melt which is in equilibrium with 1 atm of oxygen. Therefore, the activity of  $\text{Ag}_2\text{O}$  is given simply by  $\sqrt{P_{\text{O}_2}}$  when  $P_{\text{O}_2}$  is expressed in terms of atmosphere. The diameter of the silver crucible is 2 cm, and it is 4 cm deep. The sample in the crucible was maintained at the desired temperature in a tubular resistance furnace. An oxygen-nitrogen gas mixture was bubbled through the silver tube into this sample. The rate of the reaction (1) is very slow to the right direction, since the reaction proceeds one-dimensionally along the circle where the three phases are in contact. On the other hand, the backward reaction proceeds two-dimensionally on the surface of the melt, where the excess silver precipitates from the melt. The preliminary experiments showing this situation are represented in Fig. 1. The backward reaction required only about 20 hr, while it took more than 100 hr for the forward reaction to approach equilibrium. Therefore, the solubility of  $\text{Ag}_2\text{O}$  was measured mostly from the backward reaction.

## Results and Discussion

(1)  **$\text{Ag}_2\text{O}$ - $\text{B}_2\text{O}_3$  Binary System.** Figure 2 shows the activity of  $\text{Ag}_2\text{O}$  as a function of the composition of  $\text{Ag}_2\text{O}$  at a constant temperature. The dotted curve represents the Willis and Hennesy data at  $850^\circ\text{C}$ . It should be noted first that the solubility of silver oxide increases with the oxygen pressure in accordance with Eq. (1). The curve of Willis and Hennesy agrees fairly well with that of the present binary system.

The partial-molar Gibbs free energy of the solution of  $\text{Ag}_2\text{O}$  is obtained from the relation:

$$\bar{G}_{\text{Ag}_2\text{O}} = RT \ln a_{\text{Ag}_2\text{O}} \quad (3)$$

$\bar{G}_{\text{Ag}_2\text{O}}$  is plotted in Fig. 3 as a function of the  $\text{Ag}_2\text{O}$  concentration. Here one should note that

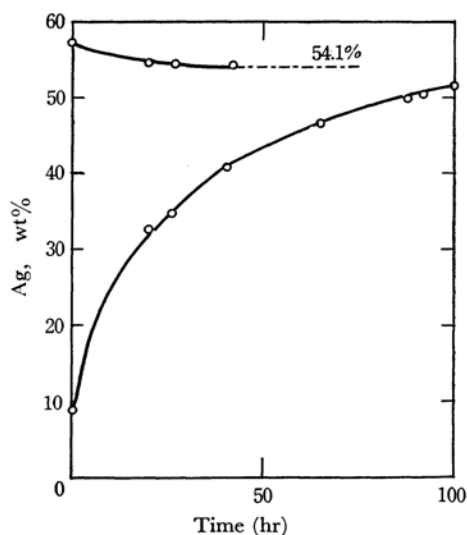


Fig. 1. Preliminary experiment of solution equilibrium of the reaction;  $2\text{Ag} + \frac{1}{2}\text{O}_2 = \text{Ag}_2\text{O}$  (in borate) at  $900^\circ\text{C}$  under 1 atm of oxygen. The equilibrium value is 54.1%.

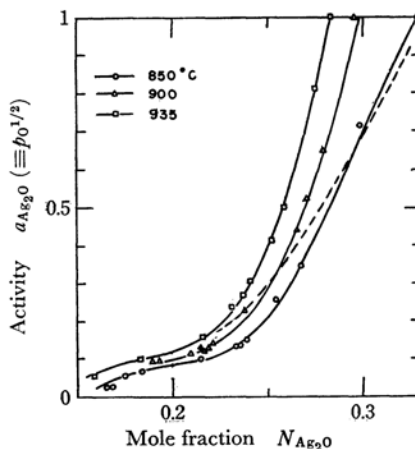


Fig. 2. The activity of  $\text{Ag}_2\text{O}$ ,  $a_{\text{Ag}_2\text{O}} (\equiv P_{\text{O}_2}^{1/2})$ , at  $850^\circ\text{C}$ ,  $900^\circ\text{C}$ , and  $935^\circ\text{C}$ . The dotted curve represents the Willis and Hennesy's data at  $850^\circ\text{C}$ . The standard state for  $\text{Ag}_2\text{O}$  is the melt in equilibrium with silver and oxygen at 1 atm.

the standard state is the solution in equilibrium with one atmosphere of oxygen.

From the temperature dependence of the partial-molar free energy of a solution, the partial-molar heat of the solution was derived; it is plotted as a function of the composition in Fig. 4. Because of the narrow temperature ranges, the values of the heat of solution are uncertain within the limits of error of  $\pm 1$  kcal/mol.

The partial molar entropy is obtained from the equation;

$$\bar{S}_{\text{Ag}_2\text{O}} = (\bar{H}_{\text{Ag}_2\text{O}} - \bar{G}_{\text{Ag}_2\text{O}})/T \quad (4)$$

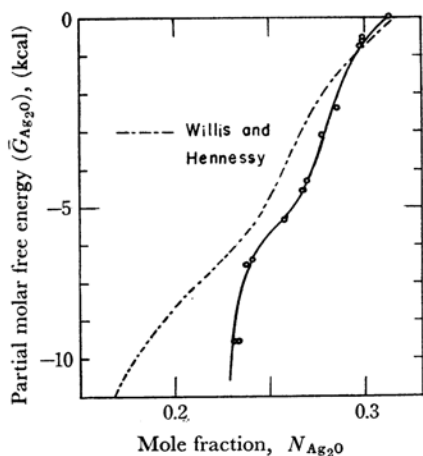


Fig. 3. Partial molar free energies of  $\text{Ag}_2\text{O}$  ( $\bar{G}_{\text{Ag}_2\text{O}}$ ) in  $\text{Ag}_2\text{O-B}_2\text{O}_3$  melts at  $850^\circ\text{C}$ . The dotted curve represents the Willis and Hennessy's data. The standard state for  $\text{Ag}_2\text{O}$ ; Silver and oxygen at 1 atm.

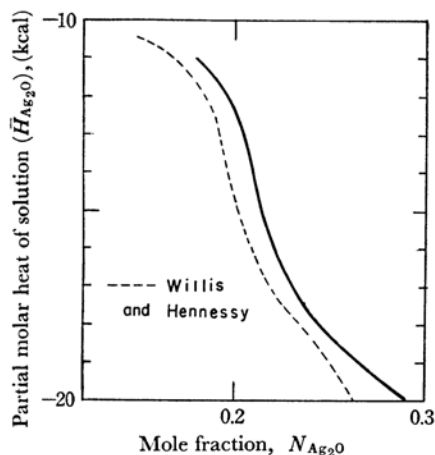
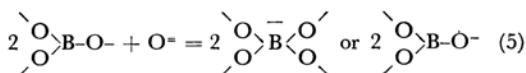


Fig. 4. Partial molar heat of solution of  $\text{Ag}_2\text{O}$  ( $\bar{H}_{\text{Ag}_2\text{O}}$ ) in  $\text{Ag}_2\text{O-B}_2\text{O}_3$  melts. The dotted curve represents the Willis and Hennessy's data. Standard state for  $\text{Ag}_2\text{O}$ : silver and oxygen at 1 atm.

it is shown in Fig. 5.

In all cases there is an inflection at  $N_{\text{Ag}_2\text{O}}=0.2$ . These phenomena indicate that the structure of Ag-borate changes significantly around this composition. In the alkaline borate melts, the destruction of the network proceeds by means of the following reaction;



The ratio of four- to three-coordinated boron atoms and the behavior of non-bridging oxygen ions, in the above reaction have been discussed

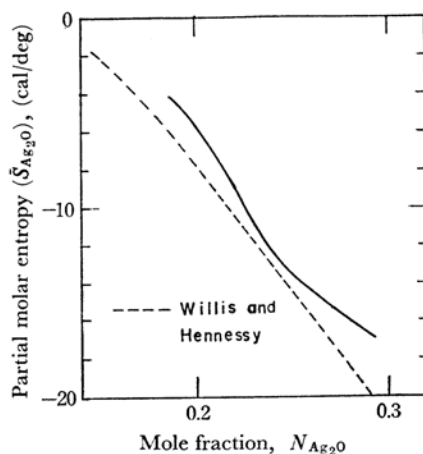


Fig. 5. Partial molar entropies of  $\text{Ag}_2\text{O}$  ( $\bar{S}_{\text{Ag}_2\text{O}}$ ) in  $\text{Ag}_2\text{O-B}_2\text{O}_3$  melts. The dotted curve represents Willis and Hennessy's data. Standard state for  $\text{Ag}_2\text{O}$ : Silver and oxygen at 1 atm.

by Beekenkamp<sup>10</sup>) in the case of alkali borate glasses. He proposed the equation;

$$N_4 = X_4(X/1-X) \quad (6)$$

where  $X_4$  is defined by;

$$X_4 = [1 + \exp(-\Delta G/KT)]^{-1} \quad (7)$$

where  $\Delta G$  is the thermodynamic potential difference between the  $\text{BO}_3\text{-M}$  unit and the  $\text{BO}_4\text{-M}$  unit, and where  $X$  is the mole fraction of alkali oxide. The same mechanism seems to be applicable in the present system. Thus, the inflection around  $N_{\text{Ag}_2\text{O}}=0.2$  can be explained in terms of the equilibrium of the  $\text{BO}_3$  unit and  $\text{BO}_4$ . If one follows the above line of approach, these experimental results seem to show that the formation of four-coordinated boron atoms is predominant to  $N_{\text{Ag}_2\text{O}}=0.2$ , while after this composition non-bridging oxygen ions gradually begin to be formed.

The infrared absorption spectra<sup>11</sup>) and the electric conductivity<sup>12</sup>) in the  $\text{Ag}_2\text{O-B}_2\text{O}_3$  system, which have been determined in our laboratory, also support this view.

(2)  **$\text{Ag}_2\text{O-Na}_2\text{O-B}_2\text{O}_3$  Ternary System.** Figure 6 shows the square root of the oxygen partial pressure, *i. e.*,  $a_{\text{Ag}_2\text{O}}$ , as a function of the composition, it also shows the  $\text{Na}_2\text{O}$  content at  $850^\circ\text{C}$ . The iso-activity lines in the  $\text{Ag}_2\text{O-Na}_2\text{O-B}_2\text{O}_3$  ternary composition diagram are shown in Fig. 7. The solubility of silver oxide decreases with an

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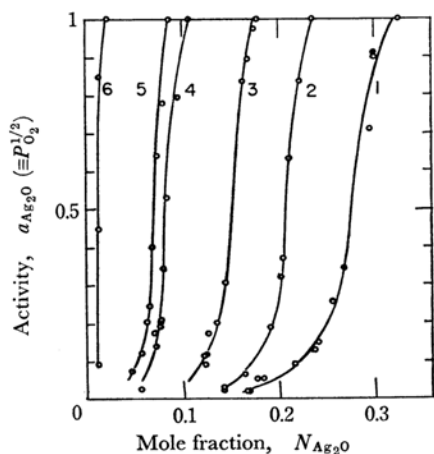


Fig. 6. The activity of  $\text{Ag}_2\text{O}$ ,  $a_{\text{Ag}_2\text{O}}$  ( $\equiv P_{\text{O}_2}^{1/2}$ ), at  $850^\circ\text{C}$  as a function of  $\text{Na}_2\text{O}$  contents. Curve 1, 2, 3, 4, 5, and 6 refer respectively to the ratio of  $N_{\text{Na}_2\text{O}}/N_{\text{B}_2\text{O}_3} = 0, 1/18, 1/9.0, 1/5.0, 1/4.8,$  and  $1/2$ .

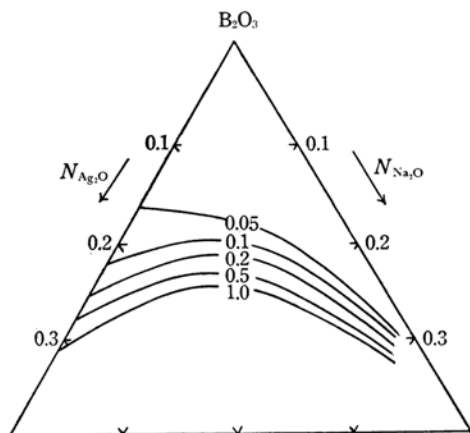
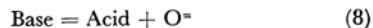


Fig. 7. The iso-activity lines of  $\text{Ag}_2\text{O}$  in  $\text{Ag}_2\text{O}$ - $\text{Na}_2\text{O}$ - $\text{B}_2\text{O}_3$  ternary composition diagram at  $850^\circ\text{C}$ .

The standard state for  $\text{Ag}_2\text{O}$  is the melt in equilibrium with silver and oxygen at 1 atm.

increase in the  $\text{Na}_2\text{O}$  contents. This indicates that the silver oxide is a weaker base than sodium oxide. This is due to the fact that, while the silver ion and the sodium ion are both monovalent and are comparable in their ionic radii, the silver ion has a large polarizability and its bond to oxygen shows a somewhat covalent character. From Fig. 7 the following fact is shown: when the  $\text{Ag}_2\text{O}$  contents are small, the  $a_{\text{Ag}_2\text{O}}$  value increases with the increase in the  $\text{Ag}_2\text{O}$  contents at a constant composition of  $\text{B}_2\text{O}_3$ , but on the  $\text{Ag}_2\text{O}$ -rich side the inverse relation occurs. This might be explained by a possible strong negative interaction among silver ions when the  $\text{Ag}_2\text{O}$  contents increase. However, this idea is not acceptable in view of

the fact that in the  $\text{Ag}_2\text{O}$ - $\text{B}_2\text{O}_3$  binary system  $\text{Ag}_2\text{O}$  behaves much like  $\text{Na}_2\text{O}$ . In molten oxide systems, it has been proposed that the strength of the base can be expressed in terms of the oxygen ion activity. This is an idea similar to that of the hydrogen ion concentration in aqueous solutions. An acid-base equilibrium was proposed by Lux and Flood to result from the following reaction;



Therefore, the higher the oxygen ion activity in a melt, the stronger its basicity. The basicity of the melts will change with the relative contents of  $\text{Ag}_2\text{O}$  and  $\text{Na}_2\text{O}$  due to the difference in the oxygen-ion activity of the two components, even in the melts with an equal composition of total basic oxides. Thus Fig. 7 shows that the oxygen-ion activity of  $\text{Ag}$ -borate is smaller than that of  $\text{Na}$ -borate. If  $\text{Ag}_2\text{O}$  and  $\text{Na}_2\text{O}$  dissociate perfectly in the melts, the following relations hold;

$$a_{\text{Ag}_2\text{O}} = a_{\text{Ag}^+}^2 \cdot a_{\text{O}^{2-}} = N_{\text{Ag}^+}^2 \cdot \gamma_{\text{Ag}^+}^2 \cdot a_{\text{O}^{2-}} = N_{\text{Ag}^+}^2 \cdot A \quad (9)$$

Here the  $A$  quantity is defined by;

$$A = a_{\text{Ag}_2\text{O}}/N_{\text{Ag}_2\text{O}} = \gamma_{\text{Ag}^+}^2 \cdot a_{\text{O}^{2-}} \quad (10)$$

where;

$$N_{\text{Ag}^+} = N_{\text{Ag}_2\text{O}}/(N_{\text{Ag}_2\text{O}} + N_{\text{Na}_2\text{O}}) \quad (11)$$

Figure 8 shows the relation between  $A$  and  $N_{\text{Ag}}$  at a constant composition of basic oxides. From Fig. 8 it may be seen that, even at a constant basic oxide composition,  $A$  increases with the increase in the proportion of  $\text{Na}_2\text{O}$  to  $\text{Ag}_2\text{O}$ . If

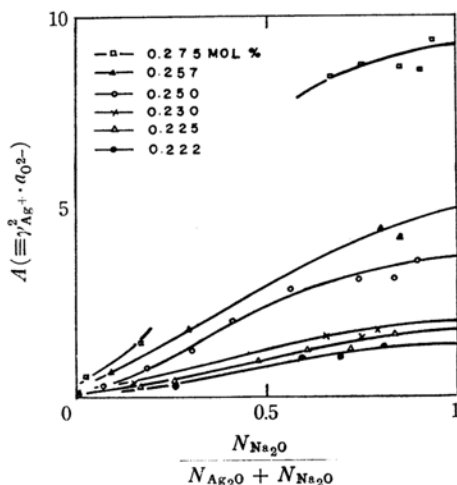


Fig. 8. The quantity  $A (= \gamma_{\text{Ag}^+}^2 \cdot a_{\text{O}^{2-}})$  as a function of  $N_{\text{Na}} (= N_{\text{Na}_2\text{O}}/(N_{\text{Ag}_2\text{O}} + N_{\text{Na}_2\text{O}}))$  at constant basic oxide concentration at  $850^\circ\text{C}$ .

it is assumed that  $\gamma_{\text{Ag}^+}$  is independent of the composition.  $A$  becomes proportional to  $a_{\text{O}^{2-}}$ .  $\gamma_{\text{Ag}^+}$  will be assumed to be constant at the lower limits

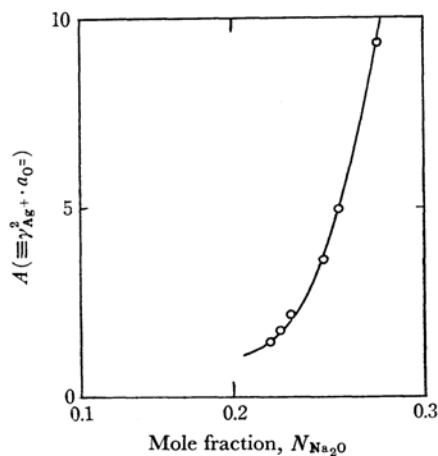


Fig. 9. The oxygen ion activity in arbitrary unit in  $Na_2O-B_2O_3$  binary melt at  $850^\circ C$ .

of the  $Ag_2O$  concentration, even though this assumption is not acceptable over the complete range of the compositions. Therefore, the value

of  $A$  extrapolated to  $N_{Ag_2O}=0$  indicates a quantity proportional to the activity of oxygen ions in the  $Na_2O-B_2O_3$  binary system. This relation is plotted in Fig. 9. The oxygen-ion activity increases rapidly with an increase in the  $Na_2O$  contents.

(3) **Metallic Silver.** It has long been considered that the silver in a glass is in a metallic colloidal state, and that this causes the coloration. However, the fact that the definite solubility exists as a function of the temperature, the oxygen pressure, and the  $Na_2O$  content shows that the silver mostly dissolves in a glass as  $Ag_2O$  as far as a thermodynamic treatment is concerned. Another piece of evidence to support this view is the electric conductivity of this system, which will be reported on a separate paper. The electrical conductance of Ag-borate is similar to that of Na-borate in its absolute value as well as in its activation energy.

The color of this glass is yellow; it turns red with the increase in the  $Ag_2O$  content. This coloration is probably due to the covalent character of the Ag-O bond.